Tomography of the Earth's atmosphere by the spaceborne occultation radiometer ORA: Spatial inversion algorithm

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Abstract. The occultation radiometer ORA was designed to perform measurements of O₃, NO₂ , H₂O, number density, and aerosol extinction altitude profiles in the Earth's atmosphere through the occultation method viewing the full solar disk. The experiment was mounted on the EURECA satellite and measured the relative transmission of light during about 7000 orbital sunsets and sunrises from August 11, 1992, to May 13, 1993. The spatial inversion algorithm developed to retrieve the total extinction altitude profiles from these data is described here. It is shown that the signal measured by an instrument having a large field of view can be successfully processed to give a much better altitude resolution than the one related to the angular size of the Sun. The main difficulties concern the inclusion of all refractive effects, the application of a new inversion scheme and its associated mapping strategy to refine the aerosol layer detection. The algorithm applies to fully nonlinear occultation experiments requiring global and nonheuristic inversion schemes.

1. Introduction

In recent years, diverse remote sensing methods, e.g., SAGE [Mauldin et al., 1985], HALOE [Russell et al., 1993], CLAES [Roche et al., 1993], have been developed for the measurement of minor constituent and aerosol vertical profiles in the Earth's atmosphere from spaceborne instruments. One approach, the occultation technique or limb tomography [Roble and Hays, 1972], relies upon measurement of the relative transmission of the light emitted by an extraterrestrial source (usually the Sun) through the atmosphere as the satellite enters or leaves the Earth's shadow along its orbit (see Figure 1). Besides the possibility of working with high spectral selectivity, the method has a fundamental advantage: it is self-calibrating, i.e., the information is extracted from the relative intensity with respect to the unattenuated intensity.

The European Retrievable Carrier (EURECA) satellite was launched by the European Space Agency (ESA) in July 1992 for a 1-year mission. For this mission, the Belgian Institute for Space Aeronomy developed a simple UV-visible radiometer (named ORA for "Occultation RADIometer") for the purpose of measuring O₃, NO₂, H₂O and aerosol extinction altitude profiles. It was accompanied by an infrared radiometer designed by the Department for Atmospheric, Oceanic and Planetary Physics of the University of Oxford to measure upper atmospheric water vapor [Calcutt et al., 1993].

The ORA instrument has been described elsewhere [Arijs et al., 1995]. Briefly, it consists of eight independent radiometers of similar design, each containing a quartz window, an interference filter, and a simple optics followed by a photodiode detector. The nominal operating wavelength of the modules and the related atmospheric major constituents are summarized in Table 1. From August 1992 to May 1993 the instrument measured about 7000 sunrises and sunsets from its quasi-circular orbit at an altitude of 508 km.

The low-orbit inclination of the satellite (28°) limited the latitude coverage between 40°S and 40°N. Owing to the minimal acceleration level requirements of the carrier, mainly dedicated to microgravity studies, and to the power and weight constraints, no Sun-pointing or scanning system coupled with a telescope was integrated to the ORA instrument. Instead, its line of sight was aligned with the optical axis of the Sun-tracking system of the satellite, which had a pointing accuracy of only 1°. Therefore, to guarantee a full view of the solar disk, a ±2° optical field of view for the ORA modules was chosen. This means that the angular extension of the sampled atmospheric region during the occultation was defined by the apparent angular size of the Sun itself (about 0.5°, representing 25 km along the vertical direction).
Any occultation experiment has to face the so-called inverse problem of retrieving the attenuation altitude profile that gave rise to the measured signal. In particular, ORA had a low spatial resolution, theoretically compensated, however, by a very large signal to noise ratio. This peculiar situation made it a challenge to construct a fast and robust algorithm capable of reconstructing the number density altitude profiles. The inverse problem can be divided into two parts. The spatial inversion concerns the retrieval of the total extinction coefficient as a function of altitude from the measured signals. On the other hand, the spectral inversion deals with the retrieval of the constituent number densities, at each altitude, using the total extinction coefficients in all channels simultaneously.

The purpose of this paper is to outline the different problems encountered in the data reduction and to explain the principles of the new spatial inversion method we developed to this end. As is explained below the spectral inversion scheme will be described in a forthcoming paper.

### 2. Formulation of the Signal

At any moment during the occultation and for a weakly refracting atmosphere there exists a one-to-one relation between the time and the trajectory of a ray issued from a particular point on the Sun and passing above the Earth's surface at an altitude $h$. In the single scattering regime and for monochromatic radiation at wavelength $\lambda$ the transmitted relative intensity through the atmosphere is

$$T_\lambda(h) = \exp \left( - \int_{s_1}^{s_2} \beta_\lambda[z(s)] \, ds \right) \quad (1)$$

where $s$ is the length element along the optical path crossing the atmosphere and $\beta_\lambda$ is the total attenuation coefficient which is supposed to be only a function of the local altitude $z$. This coefficient can be decomposed in contributions of different scatterers or absorbers, depending on the channel nominal wavelength:

$$\beta_\lambda = \beta_\lambda^{\text{Rayleigh}} + \beta_\lambda^{\text{Aerosol}} + \beta_\lambda^{O_2} + \ldots \quad (2)$$

where the superscript "Rayleigh" refers to the molecular light scattering by the air.

Considering that the instrument collects rays coming from the whole solar disk, we obtain for the total relative signal at wavelength $\lambda$

$$S_\lambda(h) = \int_{\Delta \Omega} W(\Omega) T_\lambda[h(\Omega)] \, d\Omega \quad (3)$$

Here $\Delta \Omega$ represents the solid angle domain spanned by the apparent Sun, while $W(\Omega)$ expresses the relative light distribution across the solar disk. The total measured signal is finally obtained through integration over the wavelength bandwidth of the filter to include filter characteristics and detector sensitivity as well as the solar spectral distribution:

$$S(h) = \int_{\Delta \lambda} S_\lambda(h) \, d\lambda \quad (4)$$

There is a simple relation between the attenuation coefficient for a particular constituent $X$ at wavelength $\lambda$ and the number density $n[X]$ of this constituent:

$$\beta_\lambda^{[X]}(z) = \sigma_\lambda n^{[X]}(z) \quad (5)$$

where $\sigma_\lambda$ is the effective total cross section for the considered attenuation process. It is very important to note that the latter relation is not true for aerosols, for which it is well known that the particle size distribution is broad. The aerosol scattering cross section which is clearly dependent on the particle typical size $r$ (for a given shape and chemical composition) can be written as

$$\beta_\lambda^{\text{Aerosol}} = \int_0^{\infty} \sigma_\lambda(r) \frac{dn^{\text{Aerosol}}}{dr} \, dr \quad (6)$$

where $dn^{\text{Aerosol}}/dr$ stands for the aerosol size function.

### Table 1. Major Light Absorbers at the Different UV-Visible Channels

<table>
<thead>
<tr>
<th>$\lambda$, nm</th>
<th>Predominant Constituent</th>
</tr>
</thead>
<tbody>
<tr>
<td>259</td>
<td>O$_3$, air</td>
</tr>
<tr>
<td>340</td>
<td>air, aerosols</td>
</tr>
<tr>
<td>385</td>
<td>aerosols, NO$_2$</td>
</tr>
<tr>
<td>435</td>
<td>aerosols, NO$_2$</td>
</tr>
<tr>
<td>442</td>
<td>aerosols, NO$_2$</td>
</tr>
<tr>
<td>600</td>
<td>O$_3$, aerosols</td>
</tr>
<tr>
<td>943</td>
<td>H$_2$O, aerosols</td>
</tr>
<tr>
<td>1013</td>
<td>aerosols</td>
</tr>
</tbody>
</table>
It should be well understood that occultation experiments only give access to $\beta$ while any aerosol number density derivation presupposes both an optical model (like Mie scattering) and the knowledge of the particle size distribution.

3. Optical Computations

3.1. Ray Tracing

From equation (1) it is evident that the first task of the retrieval procedure was to compute the optical path associated with all detected solar rays. This is a simple job only for grazing heights above 40 km, where refraction by the Earth’s atmosphere becomes negligible. Starting from astronomical ephemerides and the measured satellite state vector in a geocentric reference frame, the geometrical grazing height $g$ (i.e., defined by the straight line joining the Sun and the detector) is computed by considering the Earth as a standard ellipsoid. At the grazing point the surface of the Earth is approximated by a sphere tangent to the ellipsoid with the same curvature.

It is clear that the gradient of refraction index (proportional to air density) is much more important along the local vertical than along any orthogonal direction. It is a good approximation to consider that the refraction index $N(R)$ has only a radial dependence and that the light trajectory lies in the refraction plane containing the emitter Sun point, the center of the approximating sphere and the satellite. The ray path obeys the following differential equation [Born and Wolf, 1993]

$$\frac{dR}{d\theta} = \pm \frac{R}{K} \cdot \sqrt{N^2(R) R^2 - K^2} \tag{7}$$

where $\theta$ is the polar angle in the refraction plane and the turning point is defined by $dR/d\theta = 0$. Bouguer’s law expresses the momentum conservation as

$$K = || \hat{R} \times \hat{N} \hat{S} || = \text{const} \tag{8}$$

where $\hat{S}$ is the unitary vector tangent to the trajectory. Consequently, the angle defining the penetration of a ray in the atmosphere determines the value of $K$, which in turn, determines the grazing altitude.

We recognize here a boundary value problem because the position of the satellite is known but not the angle under which the ray enters the instrument. Therefore the full problem has been solved iteratively by a shooting method using a classical Runge-Kutta scheme with variable step size to integrate (7) [Press et al., 1992].

The solution trajectory was recorded as an array of optical segments. It has been chosen to divide the Sun disk into horizontal slices to represent its angular extension, assuming that refraction acts uniformly in the orthogonal direction to the refraction plane. A division of 20 slices was found to give a sufficient accuracy in the angular integration (see 3). The whole procedure was repeated for about 100 orbit positions occupied during the occultation and produced a 2 M-byte optical segment file to be passed to the spatial inversion module.

3.2. Refractive Effects

Refraction in the atmosphere actually produces several effects in an occultation experiment. Refraction not only increases the true grazing height $h$ up to 14 km (for a tangent geometrical path), but it also bends the rays (up to 1° i.e., twice the Sun’s diameter), shifting the occultation time period (up to 20 s) before geometrical sunrise or after geometrical sunset. Furthermore, the optical path length is increased in the absorbing medium.

The atmosphere can be viewed as a kind of diverging lens [Garriott, 1979] where the bending of the rays increases (however, not linearly) as they get closer to the surface. The image of the Sun through the atmosphere is consequently affected by refraction because rays coming from the "bottom" are more refracted than those coming from the "top", which results in Sun flattening (typical values are 15% at 30 km, 38% at 20 km, and 69% at 10 km). Sun flattening is also associated with a less intuitive phenomenon: the refractive dilution effect.

We want to give here an approximate description of the latter effect, assuming an infinitely thin atmosphere (in the refraction plane). This is a reasonable assumption in view of the distance between the satellite and the grazing point (~2500 km) and also because of the exponential decay of the air density with a 7-km scale height. This is equivalent to recognizing that most of the refraction occurs in a narrow region around the grazing point. For the sake of simplicity, we also consider a unidimensional Sun (see Figure 2). A ray emitted from the Sun point $Y$ can be represented by a straight line having a slope $M$ until it crosses the atmosphere at $z = 0$, where refraction takes place. The refracted ray reaches the satellite with a different slope $m$, given by

$$m(z) = M(z) + \Delta m(z) \tag{9}$$
Figure 2. Unidimensional model for refractive dilution. Rays are emitted from the Sun at \( x = L \), while refraction is assumed to occur at the grazing point \( x = 0 \). Trajectories are bent with a slope change depending on the local altitude \( z \). The ray pencils hit the satellite plane at \( x = -l \).

where \( z \) is the altitude of the crossing. Considering the Sun-Earth and Earth-satellite distances \( (L \) and \( l \), respectively), we have

\[
M = \frac{Y - z}{L} \quad \text{(10)}
\]

\[
m = \frac{z - y}{l} \quad \text{(11)}
\]

\[
(L + l)z = L + Y + l \Delta m(z) \quad \text{(12)}
\]

The energy flux \( \Phi \) hitting a plane containing the satellite and orthogonal to the refraction plane is equal to the sum of the fluxes contained in all pencils of rays emitted from the Sun and reaching an infinitesimal length element \( \Delta y \) centered on \( y \). If \( M^+ \) and \( M^- \) are the slopes of the extreme rays falling on \( \Delta y \) for the pencil emitted from \( Y \) and if \( |M| \ll 1 \), the energy flux contained in this pencil is clearly proportional to \( (M^+ - M^-) \), and the total flux is

\[
\Phi = \lim_{\Delta y \to 0} \left[ C \int_{Y_1}^{Y_2} \frac{(M^+ - M^-)}{\Delta y} \, dY \right] = \left[ C \int_{Y_1}^{Y_2} \frac{\partial M}{\partial y} \, dY \right] \quad \text{(13)}
\]

where \( C \) is an appropriate constant factor and the bounds \( Y_1 \) and \( Y_2 \) define the solar disk. Keeping \( Y \) fixed for awhile, we have

\[
\frac{\partial M}{\partial y \mid Y} = - \frac{1}{L} \frac{\partial z}{\partial y \mid Y} \quad \text{(14)}
\]

where \( y \) is the satellite position on a screen where we want to evaluate the solar flux. On the other hand, it follows from (12) that

\[
\frac{\partial z}{\partial y \mid Y} = \frac{L}{l + L} + \frac{L}{l + L} \frac{d\Delta m(z)}{dz} \frac{\partial z}{\partial y \mid Y} \quad \text{(15)}
\]

leading to

\[
\Phi = \left[ C \int_{Y_1}^{Y_2} \frac{dY}{L + l - L \frac{d\Delta m(z)}{dz}} \right] \quad \text{(16)}
\]

When \( Y \) is varying and \( y \) is constant, the total differential of (12) is

\[
(L + l) \, dz = l \, dY + L \, l \, d[\Delta m(z)] \quad \text{(17)}
\]

Combining now equations (16) and (17), we get for \( \Phi \),

\[
\Phi = \left[ C \int_{Y_1}^{Y_2} \frac{1}{l + L} \frac{dY}{dz} \right] = \left[ \frac{C}{l} \Delta z \right] \quad \text{(18)}
\]

This means that the energy flux reaching the detector will be proportional to the apparent size of the source for the above-mentioned hypothesis. The effect is far from being negligible, in view of the importance of the Sun flattening, and we have corrected the transmission signal for each Sun slice.

4. Spatial Inversion Problem

Inspection of equations (1)-(4) shows that it is not possible to directly separate the different extinction coefficients as expressed by equation (2) by taking the logarithm of the relative transmission to get the optical thickness. This is only allowed for instruments having a field of view much smaller than the Sun angular size and for which the \( W(\Omega) \) function looks like a Dirac delta function. This is a real problem because different constituents have different contributions at separate wavelengths, as for instance, air density or aerosol. Furthermore, the relative importance of these contributions may vary with altitude. It would hence be unrealistic to develop, in the case of ORA, an algorithm capable of retrieving the altitude extinction profiles ("spatial inversion") and simultaneously the associated constituents ("spectral inversion").

Accordingly we decided to perform the spatial inversion first, as it is described in this paper, being aware that high inversion residuals could impair spectral inversion for minor constituents. On the other hand, this dichotomy makes the spatial resolution analysis easier, while the full spectral inversion algorithm can be tackled independently afterward.

Because of the nonlinearity of the spatial inversion and the consequent use of iterative methods until convergence, the globality of the obtained solution should always be investigated. This means that the robustness of the algorithm has to be checked against the first-guess profile choice and the influence of outlying data points. As a systematic, although vague, criterion, we always required the solution to be not too far from expected. This somewhat arbitrary choice is nothing more than the use of a priori information that is unavoidable in solving this kind of problem, for which there are no theorems about the number of solutions.
A completely independent question concerns the large overlap between two consecutive measurements on the orbit (typical by Δh ≈ 1 km) due to the large field of view of the instrument. This causes a systematic ill-conditioning (in linear or nonlinear problems) because each measurement is close to the preceding one and can only bring new information if the signal to noise ratio is high. Indeed, the angular integration smooths the altitude profile structures out, but the signal gets higher so that its derivatives may contain signatures of these structures. The true spatial resolution of ORA for the total attenuation profile is therefore determined not only by the field of view (poor), but also by the signal to noise ratio (good, because the whole solar disk is seen) and also by the profile morphology itself (smooth for air, sharp for aerosol or ozone).

In a recent work [Fussen, 1995], we described the inadequacy of well-known heuristic methods to solve inverse problems with a large field of view. Onion peeling or Chahine algorithms [Chahine, 1972] suffer all of the drawbacks of adjusting the current solution locally (layer per layer) in an iterative way. They turned out to be unstable or inaccurate in the present case and they do not answer the question of solution uniqueness (see e.g. [Rodgers, 1976]. Sometimes they need to be stopped after an unpredictable number of iterations to prevent spurious profile oscillations from developing. In a recent paper, Lumpe et al. [1991] presented an elegant method to solve the problem analytically restricted, however, to a nonrefractive atmosphere.

5. The NOPE Method

The philosophy behind the natural orthogonal polynomial expansion (NOPE) method, which was described by Fussen [1995], is based upon three major ideas.

First, local methods have been abandoned in favor of a global one that would adjust the whole extinction profile after each iteration (and that would avoid intricate upward or downward error propagation analysis).

The second idea was to recognize that a good description of an altitude profile for, say, 50 atmospheric layers does not systematically require the determination of 50 parameters. An appropriate mathematical description using a smaller parameter set can meet the objectives for required accuracy. This was obviously an application for a basis of orthogonal polynomials so that we express the extinction profile as the series

\[ \beta(z) = \beta_0(z) + \sum_{i=0}^{I} \alpha_i \tilde{P}_i(z) \]  

The \( \tilde{P}_i(z) \) are orthonormal polynomials of the order \( i \), the \( \alpha_i \) are linear coefficients characterizing the solution, and \( \beta_0(z) \) is any well-defined a priori solution, constructed for example, from a standard atmosphere model and the knowledge of extinction cross sections and instrument spectral function. The expansion is truncated after \( I \) terms without problems if the convergence rate is fast enough (\( I = 10 \) was found to be a safe value to ensure convergence). The orthonormality property is related to the scalar product

\[ \int_0^\infty \tilde{P}_i(z) \tilde{P}_j(z) w(z) \, dz = \delta_{ij} \]  

where \( w(z) \) is the weight function [Abramowitz and Stegun, 1972].

The third and subtlest idea of the method was to exploit the fact that, among the infinite class of orthogonal polynomial sets defined by a \( w(z) \) function, a privileged choice could be

\[ w(z) = \frac{\beta_0(z)}{\int_0^\infty \beta_0(z) \, dz} \]  

By doing so, we constrain the orthogonal polynomial family to be very sensitive to (or to be “focused” on) altitude regions where structures are expected to occur. In Figure 3 a typical total extinction altitude profile at 600 nm is shown wherein the signature of the ozone layer is reduced to a bump on a logarithmic scale. While several authors [Twomey, 1975] warn against arbitrary use of prior knowledge, we want to underline here that NOPE systematically uses the a priori information but in a rigorous mathematical context. The special choice of \( w(z) \) is nothing more than a convergence accelerator for the expansion or a “window of interest” weighting procedure.

The final solution to the spatial inversion is finally obtained by applying a standard Levenberg-Marquardt...
minimization procedure [Press et al., 1992] to the merit function

\[ \chi^2 = \sum_{k=1}^{n} [s_k - S(\alpha_0, \alpha_1, \ldots, \alpha_4)]^2 \] (22)

where \( s_k \) is the measured signal for the \( k_m \) measurements during the occultation.

The following important points should be kept in mind:

1. If \( \beta(z) \) was equal to \( \beta_0(z) \), the solution vector would be \( \alpha' = \{1, 0, \ldots, 0\} \). It is thus expected that the actual solution has a decreasing series of \( \alpha_i \) if the actual atmosphere can be considered as a perturbed standard atmosphere. If it was very different from \( \beta_0(z) \), it would be systematically detected by inspecting the expansion convergence rate. In such a case, the remedy would be simply to correct \( \beta_0(z) \) in the appropriate way by using extra information or by increasing \( I \).

2. Orthogonality assures that the information content carried by \( \alpha_i \) is independent (and usually smaller in magnitude) than the one carried by \( \alpha_{i-1} \). As the number of basis functions is increased, the last terms of the expansion are just small corrections relative to the first terms which contain the largest structures.

3. The uniqueness problem is now addressed in the following way: we still don’t know whether there exists a better solution (local or global) for a given inversion problem but the solution obtained by NOPE should normally be the closest one to the reasonable mean state of the atmosphere defined by \( \beta_0(z) \).

6. The Inversion Procedure

For all the ORA channels we can compute \( \beta_0^{(n)}(z) \) and generate the adequate polynomial set using, for instance, a Stieltjes procedure [Press et al., 1992]. A last difficulty subsists, however, with the aerosols, for which the information concerning the wavelength dependence of the extinction profile is scarce in the post-Pinatubo period (a much flatter curve is the only dominant aspect). Furthermore, the altitude profiles may exhibit high variabilities over short time or geographical ranges [Brogniez and Lenoble, 1991].

For the ORA experiment some channels (in particular at \( \lambda = 943 \) and 1013 nm) were dominated by the still large Pinatubo aerosol effect. This caused strong attenuation (also called signal saturation), reducing the relative importance of the aerosol layer signature on the signal. Moreover, the sharp structure of the Junge layer (about 5 km full width at half maximum) could be contaminated for a large field of view instrument by a "cut-off" attenuation due to tropospheric or stratospheric clouds [Kent et al., 1993]. Therefore a simple mean exponential (monotonic) aerosol profile used to construct \( \beta_0(z) \) turned out to be inadequate and produced a local solution not capable of reproducing the signal bump characteristic of the aerosol layer. To ameliorate the result at low altitudes, we adopted the following strategy.
By simply looking at the ORA signal, we can easily detect an aerosol layer signature as a bump (or a hole) in the tail of the transmitted intensity. This information should be passed to the inversion algorithm to emphasize that region. First, we have defined a more elaborate generic aerosol profile as
\[ \beta_g(z) = c_0 \exp \left( -\frac{c_1 \delta^2 + \delta^3}{c_2 + c_3 \delta^2} \right), \quad \delta = (z - z_c) \]  
(23)
where \( \vec{V} = [z_c, c_0, c_1, c_2, c_3] \) is a vector of free parameters. With this analytic form, \( \beta_g(z) \) may (or not as the free parameters are varied) represent a maximum at the centroid \( z = z_c \) while it is always asymptotic (for high altitude) to a pure exponential behavior. The set of parameters has been varied over a large range, and about 2700 synthetic occultations have been produced as “forward” computations. The strategy consisted of an approximate mapping between the signal and the parameter set (see Figure 4). The synthetic signal can be numerically analysed, and an extremum (in the curve or in its derivatives) is detected at \( h = h_e \). Four symmetrical adjacent nodes are defined at \( h_1, h_2, h_3, h_4 \), together with the logarithm of the transmission, \( L_1, L_2, L_3, L_4 \), respectively. Let us define the vector \( \vec{U} = [L_1, L_2, L_3, L_4] \). There exists an unknown and intricate relation (otherwise the inversion problem would be trivial to solve) between every component of \( \vec{V} \) and the five components of \( \vec{U} \). For the sake of generality we expressed

Figure 6. Result of a typical inversion (October 10, 1992, 27°N latitude, 13°E longitude) for the seven wavelengths used by ORA. (top): Retrieved total extinction profiles (1 m\(^{-1}\) = 1000 km\(^{-1}\)) versus altitude (km). (bottom): Measured signal (solid line) and computed signal (crosses) derived using the corresponding profiles above. Note the evolution of the aerosol layer signature as the wavelength increases.
this relation as a full cubic form of five variables (46 coefficients) as

\[ y^V_i = \Theta^V_i(\overline{U}) \quad \{i = 1, \ldots 5\} \tag{24} \]

The matrix \( \Theta \) has been determined by a linear least-squares fit over the whole synthetic signal data set. By using (24), it is then possible to predict the used parameters with moderate accuracy (standard deviation is 0.43 km on \( x_c \) and 0.32 km on \( c_2 \)). This mapping can be used to compute a generic aerosol profile, which in turn, is added to the other extinction profiles (due to other constituents) to produce the \( w(z) \) function in each channel.

The final flowchart for the spatial inversion scheme has been summarized in Figure 5, and its completion required about \( 10^9 \) flops for each occultation event (within seven usable channels).

7. Results and Conclusions

In Figure 6 we report the final solution obtained for a typical occultation. The mean \( \xi = \sqrt{x^2/k_m} \) residual (i.e., the mean deviation between the measured transmission and the transmission obtained from the solution profile) was found to increase slightly with wavelength (\( \xi \approx 0.0010 \) at \( \lambda = 340 \text{ nm} \) to \( \xi \approx 0.0026 \) at \( \lambda = 1013 \text{ nm} \)). The value of \( \xi \) does not seem to be determined by the experimental noise (\( \sim 10^{-4} \)) but more probably by possible systematic errors in the description of the refraction processes, the discretization and interpolation schemes used for the Sun or the atmosphere and the NOPE method itself. At altitudes above 45 or 50 km, possible erratic profile behaviors can be observed which are cancellation effects between the \( x_i \) coefficients (keeping in mind the very large dynamical range of the extinction coefficients). It is evident that the mapping strategy has given a somewhat more important weight to the inversion in the region of the aerosol layer because it became an important topic. On the other hand, the occultation method is limited at high altitudes because the attenuation is too weak, and at low altitudes because it is too strong (saturation), rendering the signal insensitive to the profile. A lower bound for the minimal meaningful signal would be 1 to \( 2 \times 10^{-8} \), while information can be extracted for \( \beta(z) \) ranging between \( 10^{-5} \) and \( 10^{-1} \text{ km}^{-1} \).

A quick inspection of Figure 6 reveals that the reduced relative importance of the aerosol layer is reduced as the wavelength decreases. For \( \lambda = 600 \text{ nm} \) the aerosol peak exhibits a shoulder due to the ozone contribution. It is the purpose of the spectral inversion to extract the constituent density number by using the related cross sections in all channels.

All the occultations measured by ORA between August 1992 and May 1993 have now been fully processed and stored. In the near future we will develop the spectral inversion algorithm in parallel with the investigation of directly exploitable channels (like \( \lambda = 1013 \text{ nm} \), almost exclusively sensitive to the aerosol) and their validation with respect to other experiments. A complete error analysis will also be performed.

The spatial inversion algorithm of ORA appears to be able to retrieve extinction profiles with a much better altitude resolution than one would have expected by considering the large field of view of the instrument. The method is numerically quite expensive but nevertheless offers some warranty for the obtained solution, which some heuristic schemes do not. The condition sine qua non for such an instrument being competitive with more sophisticated experiments is, of course, the recording of a quasi noiseless signal.

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